
Compiler-Based Autotuning for Productive Parallel Programming *and its Relationship to Design Space Exploration*

Mary Hall

May, 2011

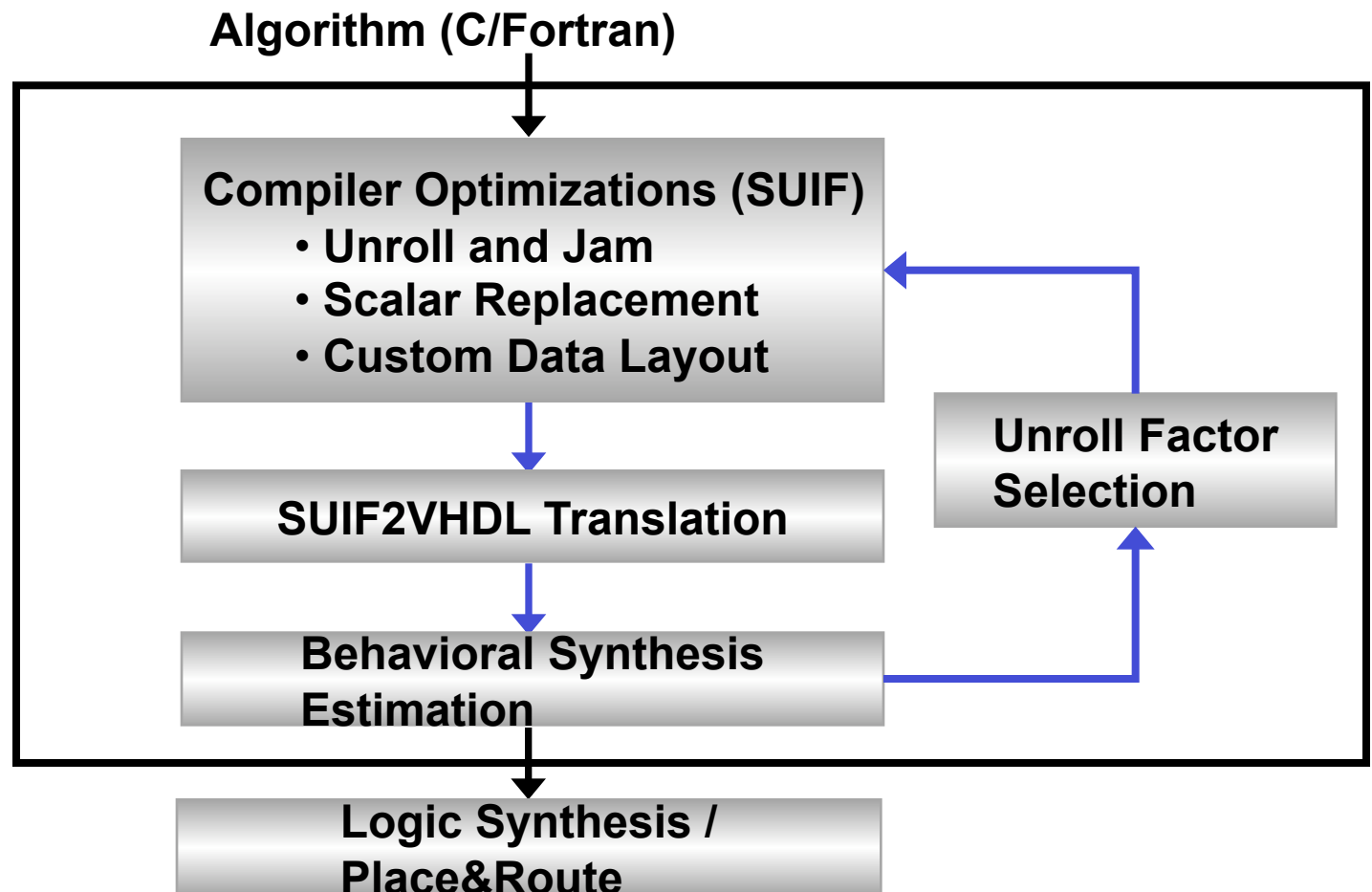
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Outline

1. FPGA design space exploration in DEFACTO
2. Related idea: Compiler-based autotuning in CHiLL and CUDA-CHiLL
3. Case study 1: specialized linear algebra for supercomputer application
4. Case study 2: linear algebra for GPUs

Automatic Design Space Exploration in DEFACTO



- ◆ Overall, less than 2 hours
- ◆ 5 minutes for optimized design selection

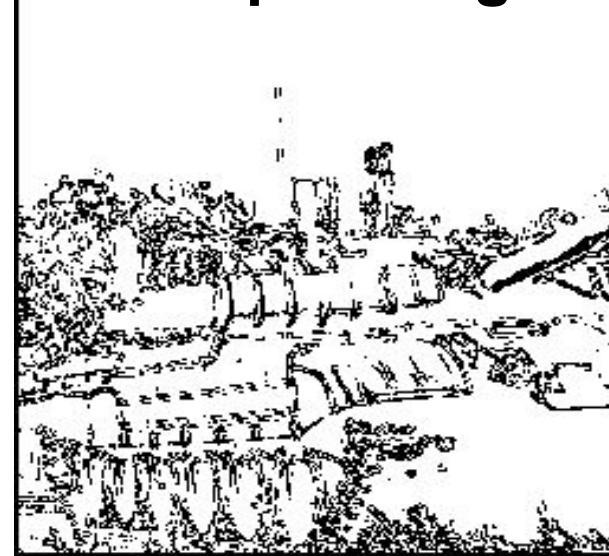
B. So, M. Hall and P. Diniz, "A Compiler Approach for Fast Design Space Exploration for FPGA-Based Systems," ACM PLDI '02, June, 2002.

Sobel Edge Detection on Annapolis Wildstar

Input Image



Output Image



Metrics	Manual	Automated
Space (slices)	2238	2279 (2% increase)
Cycles	326K	518K
Clock Rate (MHz)	42	40
Execution Time (one frame)	7.7 ms (100%)	12.95 ms (159%)
Design Time	about 1 week	42 minutes

DEFACTO Major Findings

- Performance within 2X of manual, 100X reduction in design time and automatic [M&M05].
- Design space exploration using compiler optimizations of C code, VHDL generation, then synthesis [PLDI02].
 - Unrolling to exploit parallelism, scalar replacement to manage storage, loop permutation
- Estimates from behavioral synthesis, although inaccurate, provide fast and relative guidance on design selection [DAC03].
- Extended to pipelined designs using communication analysis and design space exploration [FCCM02,DAC03,FPGA05].

DEFACTO collaborators: primarily Byoungro So, Heidi Ziegler, Joonseok Park and Pedro Diniz

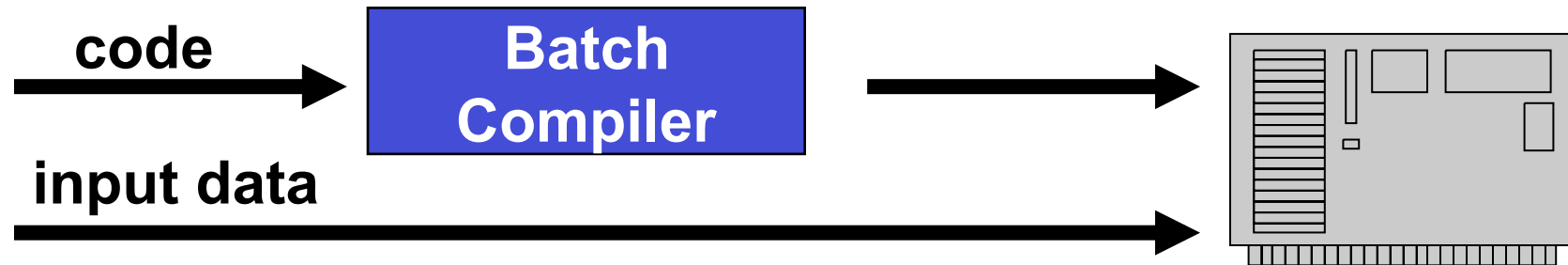
From Custom Hardware to Tuned Software

- Architectures are getting increasingly complex
 - Multiple cores, deep memory hierarchies, software-controlled storage, shared resources, SIMD compute engines, heterogeneity, ...
- Performance optimization is getting more important
 - Today's sequential and parallel applications **may not** be faster on tomorrow's architectures.
 - Especially if you want to add new capability!
 - Managing **data locality** even more important than parallelism.
 - Managing **power** of growing importance, too.

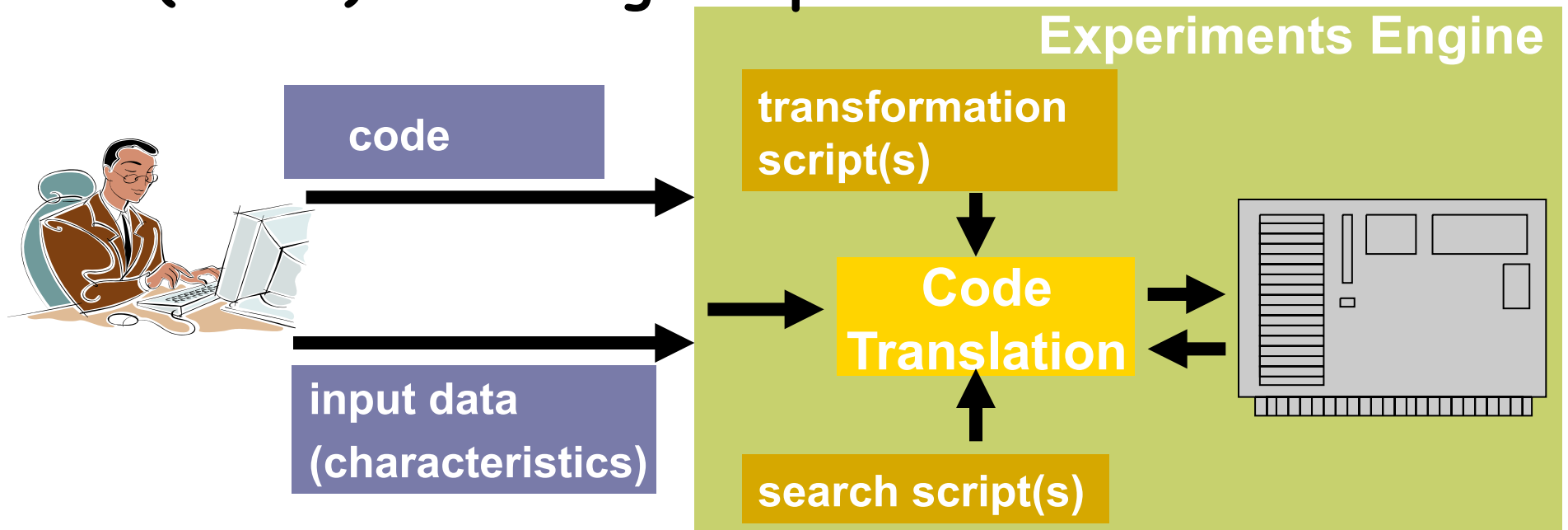
Complexity!

Motivation: Collaborative Autotuning “Compiler”

Traditional view:

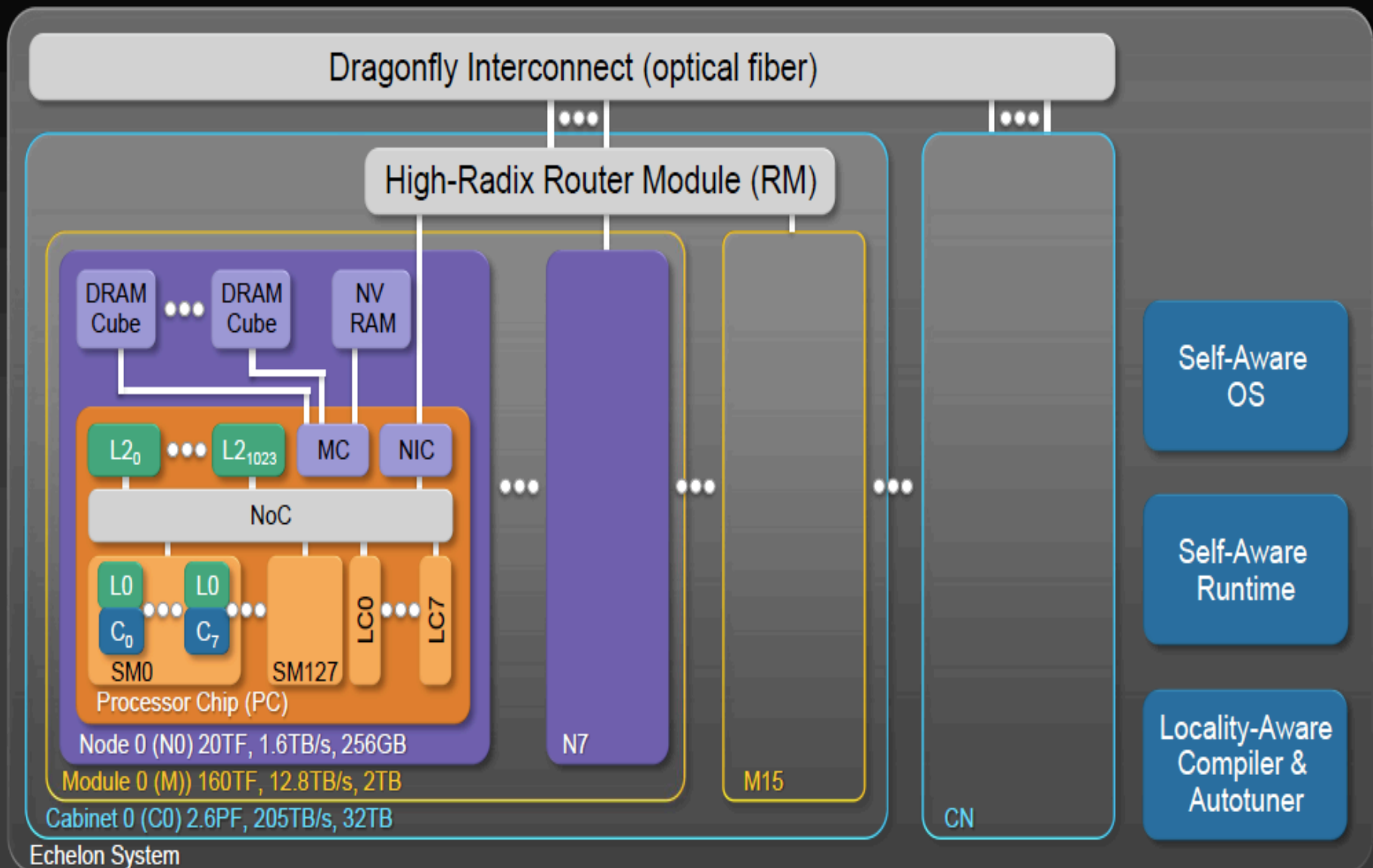


(Semi-)Autotuning Compiler:

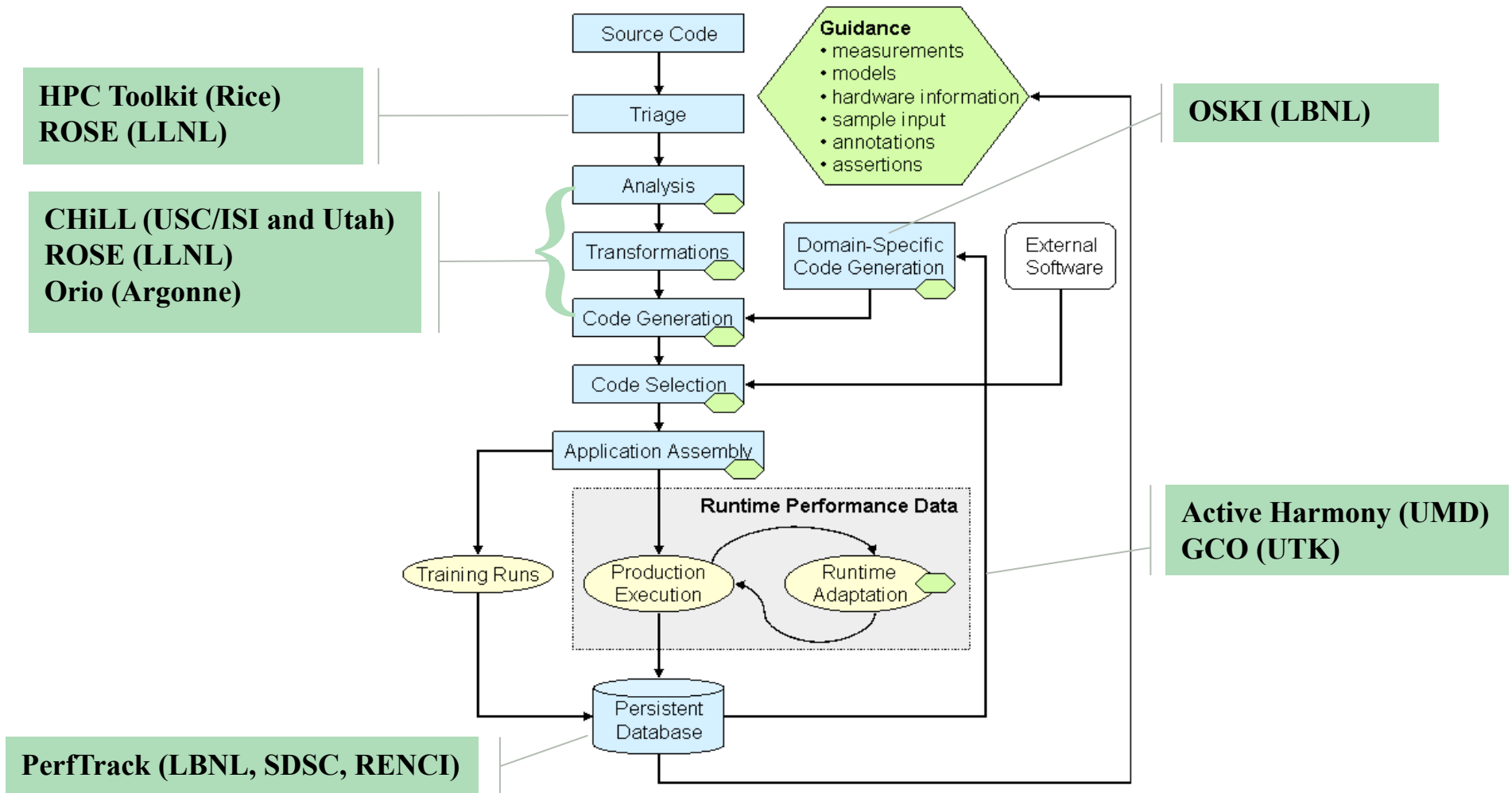


Echelon System Sketch

from "GPU Computing To Exascale and Beyond", Bill Dally, SC10



(DOE SciDAC) PERI Autotuning Tools



Autotuning and Specialization Improve Performance of Supercomputer Applications

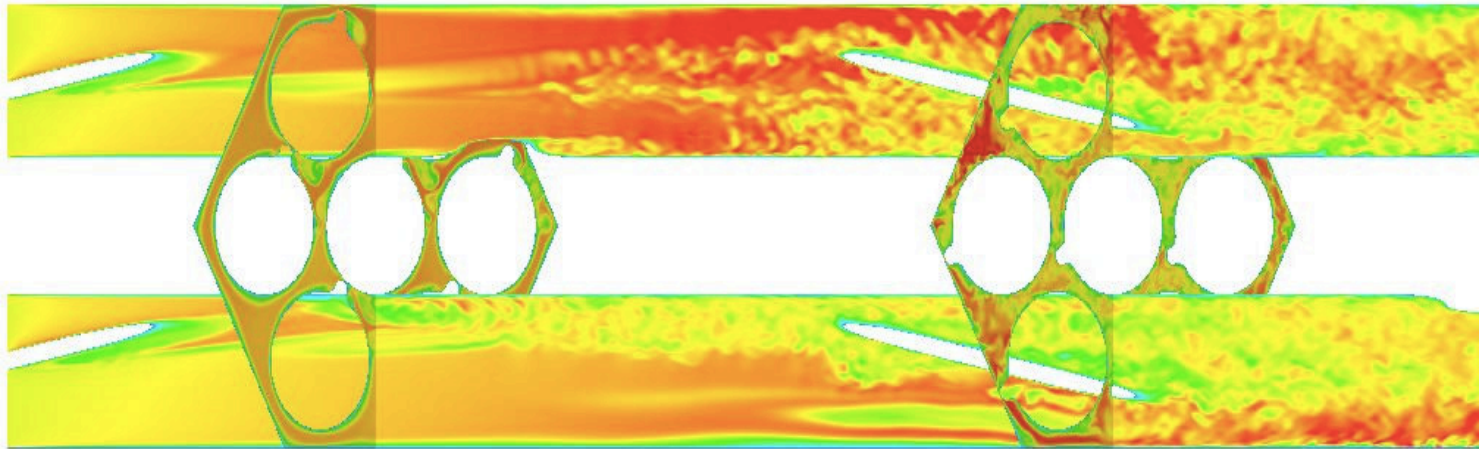
- Production scientific applications make heavy use of libraries to achieve high performance
 - E.g., BLAS, PETSc
- Using these libraries in unusual ways may be at odds with how they were optimized
- **Key Idea:** Compiler specializes library for application, and employs autotuning to achieve higher performance than manually-tuned version

Shin, Chen, Chame, Hall, and Hovland, “Autotuning and Specializing: Speeding up Matrix Multiply using Compiler Technology”, IWAPT ‘09, Oct. 2009.

Shin, Chen, Chame, Hall, Fisher and Hovland, “Autotuning and Specializing: Speeding up Nek5000 using Compiler Technology”, ICS ‘10, June 2010.

Autotuning of Nek5000

Spectral element code: turbulence in wire-wrapped subassemblies



- Applications: nuclear energy, astrophysics, ocean modeling, combustion, bio fluids,
- Scales to $P > 10,000$ (Cray XT5, BG/P)
- > 75% of time spent on manually optimized mxm
 - matrix multiply of very small, rectangular matrices
 - matrix sizes remain the same for different problem sizes

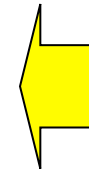
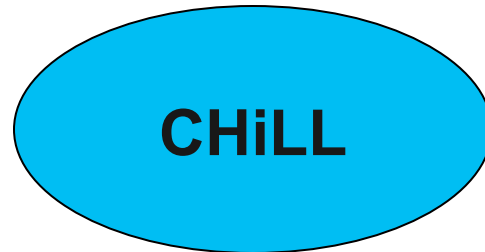
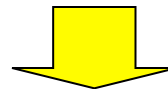
Generate Library Automatically Using CHiLL

High-level loop transformation and code generation framework

- based on polyhedral model
- script interface for programmers or compilers
- optimization strategy expressed as sequence of composable transformations

```
for(i=0; i<n; i++)  
  for(j=0; j<n; j++)  
    for(k=0; k<n; k++)  
      c[i][j]+=a[i][k]*b[k][j];
```

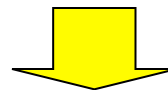
mxm.c (also supports Fortran as input)



213-122.script

source: mxm.c
procedure: 0
loop: 0

known(n=10)
permute([2,1,3])
unroll(0,2,2)
unroll(0,3,2)

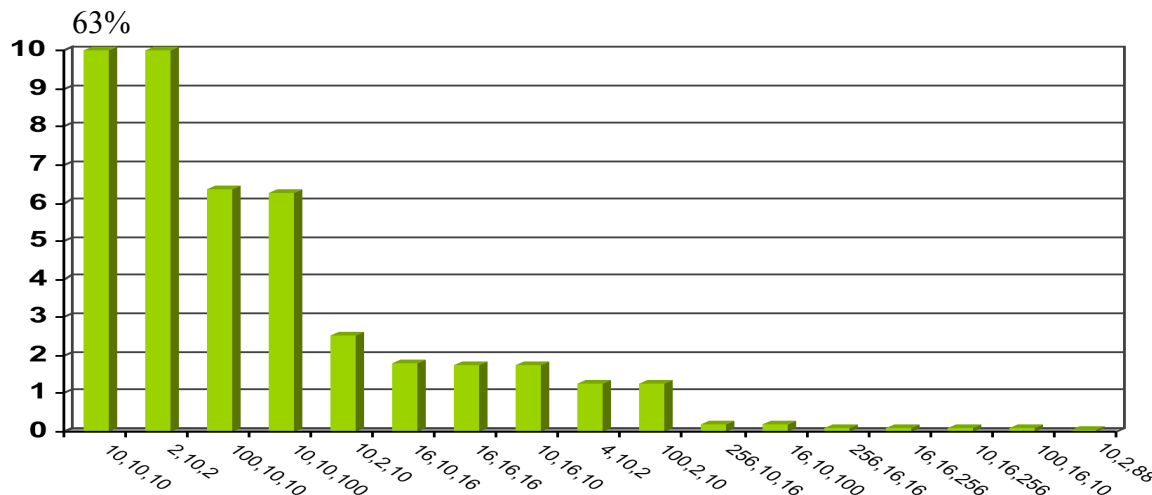


```
for(j=0; j<10; j++)  
  for(i=0; i<10; i+=2)  
    for(k=0; k<10; k+=2){  
      c[i][j]+=a[i][k]*b[k][j];  
      c[i][j]+=a[i][k+1]*b[k+1][j];  
      c[i+1][j]+=a[i+1][k]*b[k][j];  
      c[i+1][j]+=a[i+1][k+1]*b[k+1][j];  
    }
```

mxm213.out

BLAS Library is Significant to Performance

- 8 input sizes comprise 75% of time
- Optimization opportunities
 - exploit reuse in registers (**unroll-and-jam**)
 - exploit SIMD (in the Opteron SSE-3) (**permute, unroll**)
 - reduce loop overheads (**unroll, specialize**)



Generated Code: Do You Want to Write This?

Example: loop order ijk, unroll 8-4-1

```
FUNCTION M_100_10_8 (A, B, C)
```

```
  INTEGER M_100_10_8, T4, T6  
  DOUBLE PRECISION A, B, C
```

```
  DIMENSION A(8, 10)  
  DIMENSION B(10, 100)  
  DIMENSION C(8, 100)
```

```
  DO 2, T4 = 1, 97, 4
```

```
  C(1, T4) = 0.00000000000000000000D+00  
  C(1 + 1, T4) = 0.00000000000000000000D+00  
  C(1 + 2, T4) = 0.00000000000000000000D+00  
  C(1 + 3, T4) = 0.00000000000000000000D+00  
  C(1 + 4, T4) = 0.00000000000000000000D+00  
  C(1 + 5, T4) = 0.00000000000000000000D+00  
  C(1 + 6, T4) = 0.00000000000000000000D+00  
  C(1 + 7, T4) = 0.00000000000000000000D+00  
  C(1, T4 + 1) = 0.00000000000000000000D+00  
  C(1 + 1, T4 + 1) = 0.00000000000000000000D+00  
  C(1 + 2, T4 + 1) = 0.00000000000000000000D+00  
  C(1 + 3, T4 + 1) = 0.00000000000000000000D+00  
  C(1 + 4, T4 + 1) = 0.00000000000000000000D+00  
  C(1 + 5, T4 + 1) = 0.00000000000000000000D+00  
  C(1 + 6, T4 + 1) = 0.00000000000000000000D+00  
  C(1 + 7, T4 + 1) = 0.00000000000000000000D+00  
  C(1, T4 + 2) = 0.00000000000000000000D+00  
  C(1 + 1, T4 + 2) = 0.00000000000000000000D+00  
  C(1 + 2, T4 + 2) = 0.00000000000000000000D+00  
  C(1 + 3, T4 + 2) = 0.00000000000000000000D+00  
  C(1 + 4, T4 + 2) = 0.00000000000000000000D+00  
  C(1 + 5, T4 + 2) = 0.00000000000000000000D+00  
  C(1 + 6, T4 + 2) = 0.00000000000000000000D+00  
  C(1 + 7, T4 + 2) = 0.00000000000000000000D+00  
  C(1, T4 + 3) = 0.00000000000000000000D+00  
  C(1 + 1, T4 + 3) = 0.00000000000000000000D+00  
  C(1 + 2, T4 + 3) = 0.00000000000000000000D+00  
  C(1 + 3, T4 + 3) = 0.00000000000000000000D+00  
  C(1 + 4, T4 + 3) = 0.00000000000000000000D+00  
  C(1 + 5, T4 + 3) = 0.00000000000000000000D+00  
  C(1 + 6, T4 + 3) = 0.00000000000000000000D+00  
  C(1 + 7, T4 + 3) = 0.00000000000000000000D+00
```

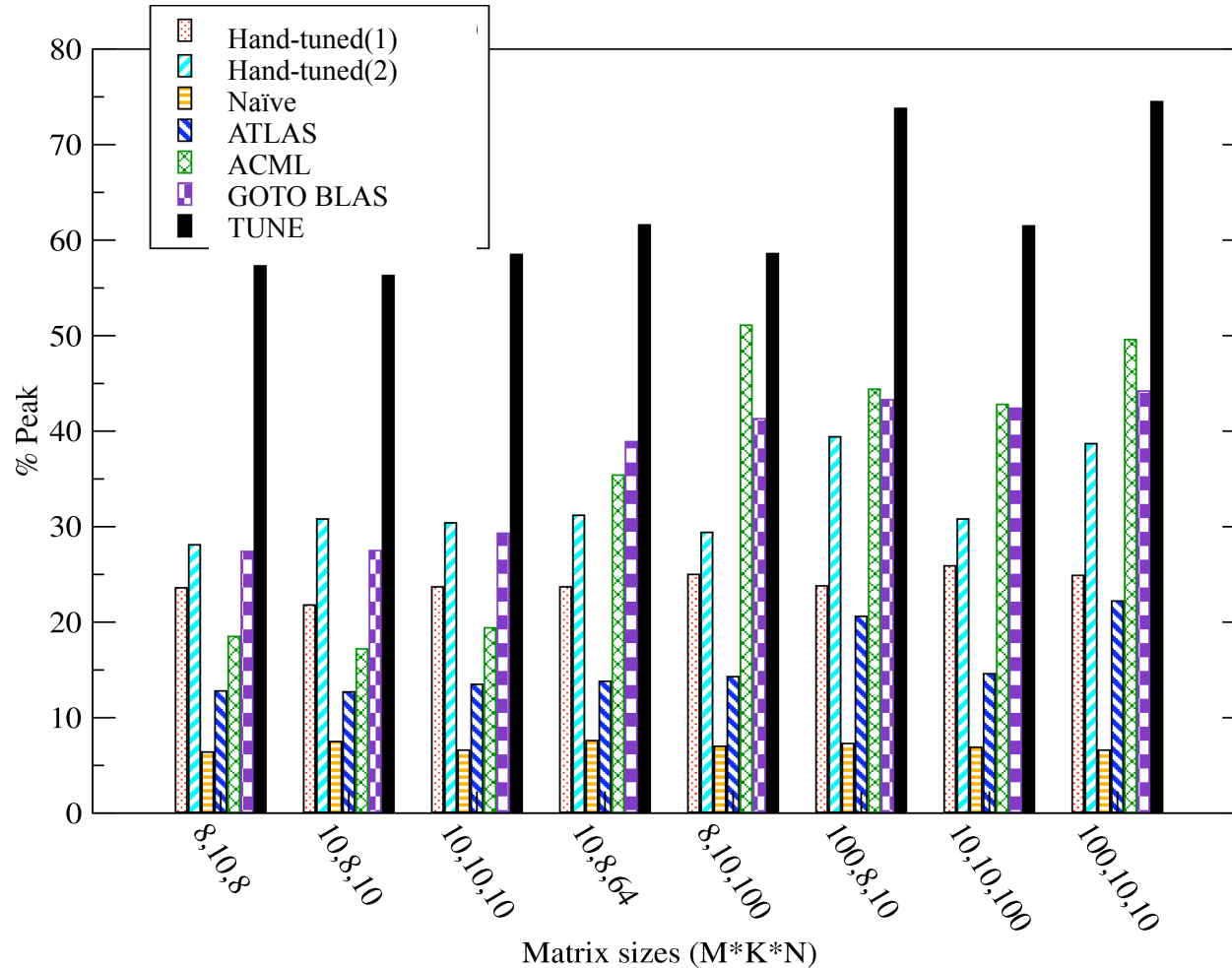
```
  DO 4, T6 = 1, 10, 1
```

```
  C(1, T4) = C(1, T4) + A(1, T6) * B(T6, T4)  
  C(1 + 1, T4) = C(1 + 1, T4) + A(1 + 1, T6) * B(T6, T4)  
  C(1 + 2, T4) = C(1 + 2, T4) + A(1 + 2, T6) * B(T6, T4)  
  C(1 + 3, T4) = C(1 + 3, T4) + A(1 + 3, T6) * B(T6, T4)  
  C(1 + 4, T4) = C(1 + 4, T4) + A(1 + 4, T6) * B(T6, T4)  
  C(1 + 5, T4) = C(1 + 5, T4) + A(1 + 5, T6) * B(T6, T4)  
  C(1 + 6, T4) = C(1 + 6, T4) + A(1 + 6, T6) * B(T6, T4)  
  C(1 + 7, T4) = C(1 + 7, T4) + A(1 + 7, T6) * B(T6, T4)  
  C(1, T4 + 1) = C(1, T4 + 1) + A(1, T6) * B(T6, T4 + 1)  
  C(1 + 1, T4 + 1) = C(1 + 1, T4 + 1) + A(1 + 1, T6) * B(T6, T4 + 1)  
  C(1 + 2, T4 + 1) = C(1 + 2, T4 + 1) + A(1 + 2, T6) * B(T6, T4 + 1)  
  C(1 + 3, T4 + 1) = C(1 + 3, T4 + 1) + A(1 + 3, T6) * B(T6, T4 + 1)  
  C(1 + 4, T4 + 1) = C(1 + 4, T4 + 1) + A(1 + 4, T6) * B(T6, T4 + 1)  
  C(1 + 5, T4 + 1) = C(1 + 5, T4 + 1) + A(1 + 5, T6) * B(T6, T4 + 1)  
  C(1 + 6, T4 + 1) = C(1 + 6, T4 + 1) + A(1 + 6, T6) * B(T6, T4 + 1)  
  C(1 + 7, T4 + 1) = C(1 + 7, T4 + 1) + A(1 + 7, T6) * B(T6, T4 + 1)  
  C(1, T4 + 2) = C(1, T4 + 2) + A(1, T6) * B(T6, T4 + 2)  
  C(1 + 1, T4 + 2) = C(1 + 1, T4 + 2) + A(1 + 1, T6) * B(T6, T4 + 2)  
  C(1 + 2, T4 + 2) = C(1 + 2, T4 + 2) + A(1 + 2, T6) * B(T6, T4 + 2)  
  C(1 + 3, T4 + 2) = C(1 + 3, T4 + 2) + A(1 + 3, T6) * B(T6, T4 + 2)  
  C(1 + 4, T4 + 2) = C(1 + 4, T4 + 2) + A(1 + 4, T6) * B(T6, T4 + 2)  
  C(1 + 5, T4 + 2) = C(1 + 5, T4 + 2) + A(1 + 5, T6) * B(T6, T4 + 2)  
  C(1 + 6, T4 + 2) = C(1 + 6, T4 + 2) + A(1 + 6, T6) * B(T6, T4 + 2)  
  C(1 + 7, T4 + 2) = C(1 + 7, T4 + 2) + A(1 + 7, T6) * B(T6, T4 + 2)  
  C(1, T4 + 3) = C(1, T4 + 3) + A(1, T6) * B(T6, T4 + 3)  
  C(1 + 1, T4 + 3) = C(1 + 1, T4 + 3) + A(1 + 1, T6) * B(T6, T4 + 3)  
  C(1 + 2, T4 + 3) = C(1 + 2, T4 + 3) + A(1 + 2, T6) * B(T6, T4 + 3)  
  C(1 + 3, T4 + 3) = C(1 + 3, T4 + 3) + A(1 + 3, T6) * B(T6, T4 + 3)  
  C(1 + 4, T4 + 3) = C(1 + 4, T4 + 3) + A(1 + 4, T6) * B(T6, T4 + 3)  
  C(1 + 5, T4 + 3) = C(1 + 5, T4 + 3) + A(1 + 5, T6) * B(T6, T4 + 3)  
  C(1 + 6, T4 + 3) = C(1 + 6, T4 + 3) + A(1 + 6, T6) * B(T6, T4 + 3)  
  C(1 + 7, T4 + 3) = C(1 + 7, T4 + 3) + A(1 + 7, T6) * B(T6, T4 + 3)
```

```
  4 CONTINUE  
  3 CONTINUE  
  2 CONTINUE  
  1 CONTINUE  
  M_100_10_8 = 0  
  RETURN
```

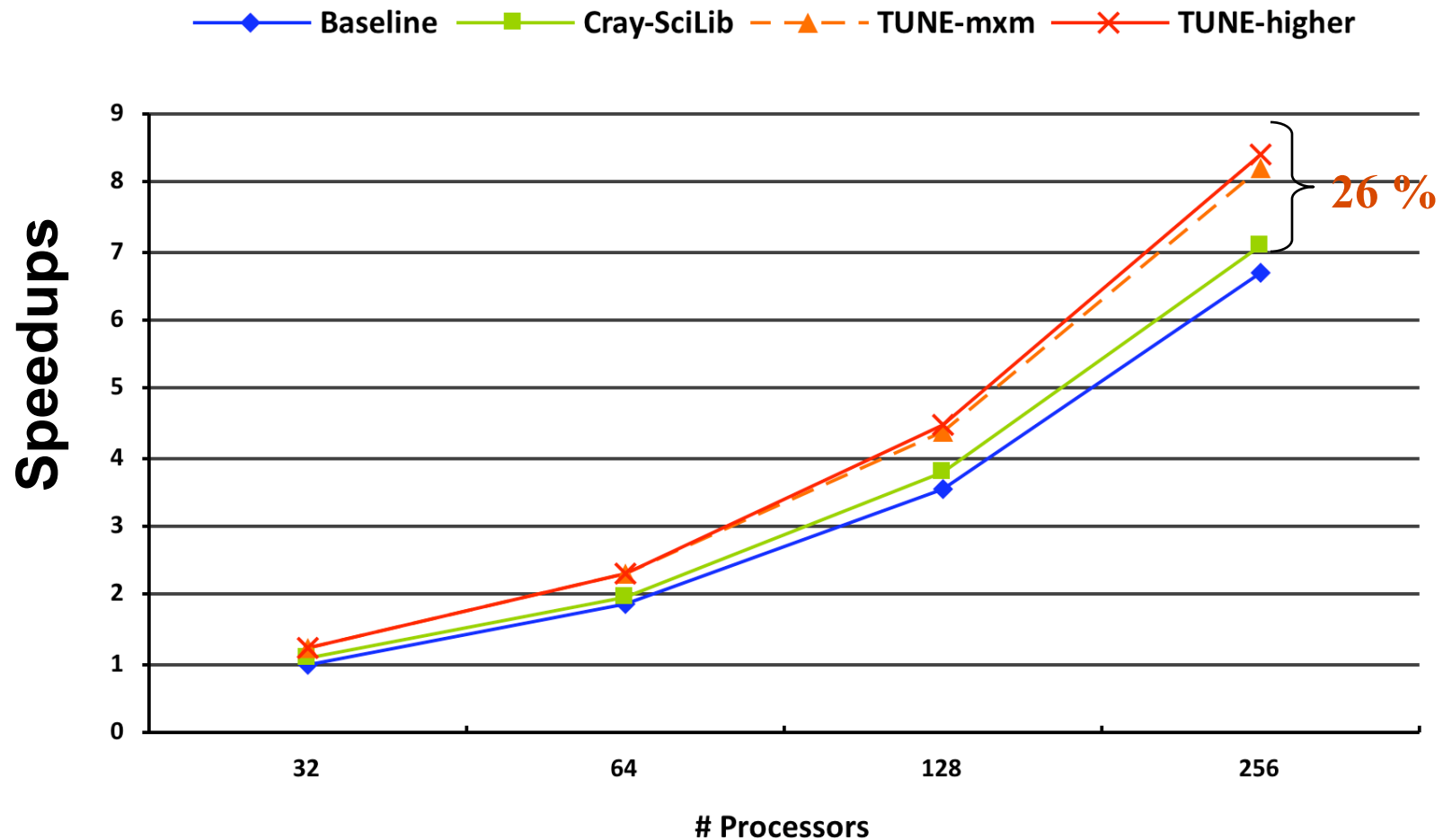
```
END
```

Automatically Generated Code is Faster than Manually-Tuned Libraries



2.2X speedup
for DGEMM
1.34X
speedup
for Nek5000

Nek5000 (g6a input) on Jaguar



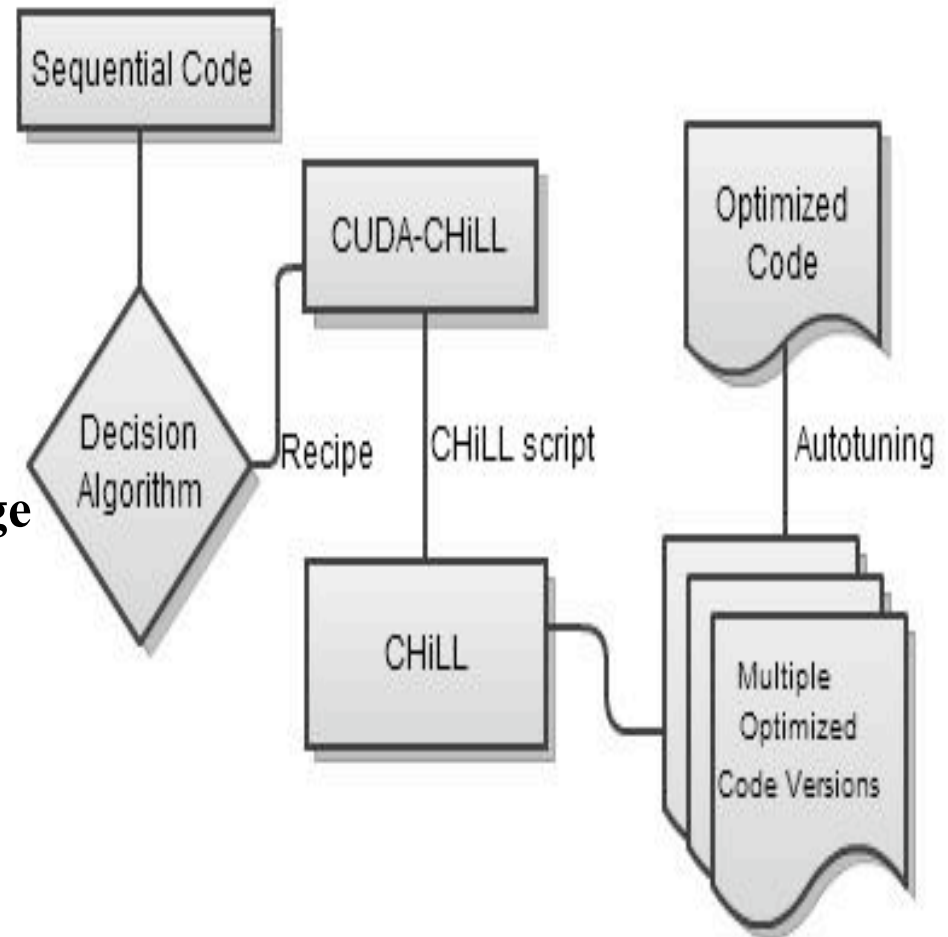
Autotuning for Future Systems

- **Future systems:** increasingly complex memory hierarchies, heterogeneous functional units
- Automatically generate CUDA for NVIDIA GPU from sequential code plus transformation recipe
- **Beyond OpenMP:** abstraction permits parallel threads & staging of data
- **Automatic parallelization:** Heuristics similar to CGO 2005 paper (Models plus heuristics plus search)
- Programming language interface provides higher levels of abstraction and permits prototyping of compiler algorithms
- **Heterogeneous code generation:** Alternative scripts generate CUDA, OpenMP or sequential code (Open CL underway) tuned for memory hierarchy

Reference: Rudy, Khan, Hall, Chen, and Chame, “A Programming Language Interface to Describe Transformations and Code Generation,” LCPC ‘10, Oct. 2010.

CUDA-CHiLL System (UPDATE)

- **Input: Sequential C Code**
- **Optimizing decisions**
 - Computational decomposition
 - Data Staging
- **Generate transformation recipe**
 - High-level programming language interface
- **Polyhedral framework**
 - Transformation and code generation
- *Cudaize* code
- Autotuning



Guiding Transformation and Code Generation with a Transformation Recipe

```
for (i=0; i<N; i++)
```

Matrix-vector Multiply Source Code:

```
for (j=0; j<N; j++)
```

```
a[i] = a[i] + c[j][i]*b[j];
```

Example CUDA-CHILL Recipe:

```
N = 1024
```

```
//Auto-tuning finds values for TI and TJ
```

```
tile_by_index({"i","j"}, {TI},  
  {l1_control="ii",l2_control="jj"},  
  {"ii","jj", "i", "j"})
```

```
//normalize loop to start at "i"=0
```

```
normalize_index("i")
```

```
cudaize("mv_GPU", {a=N, b=N,  
  c=N*N},{block={"ii"}, thread={"i"}})
```

```
copy_to_shared("tx", "b", 1)
```

```
copy_to_registers("k", "a")
```

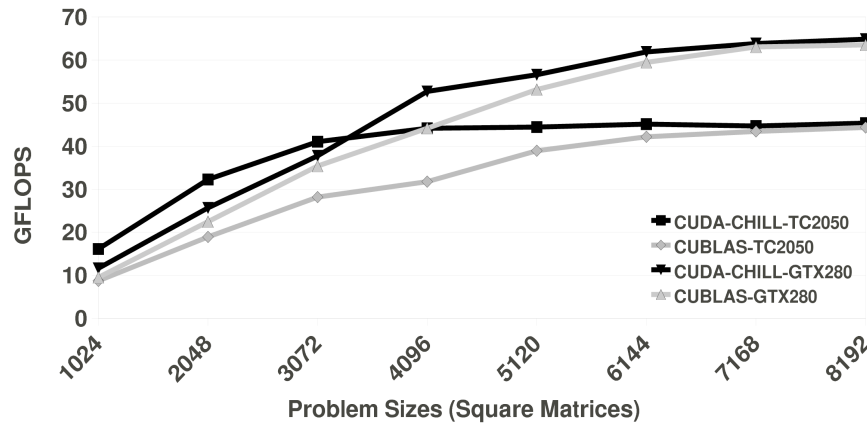
```
unroll_to_depth(1)
```

Automatically Generated Code:

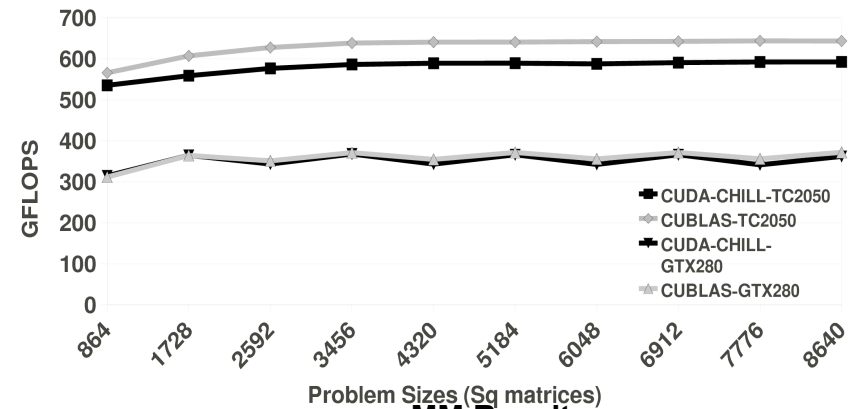
```
__global__ mv_GPU(float* a, float* b, float** c) {  
  int bx = blockIdx.x; int tx = threadIdx.x;  
  __shared__ float bcpy[32];  
  double acpy = a[tx + 32 * bx];  
  for (k = 0; k < 32; k++) {  
    bcpy[tx] = b[32 * k + tx];  
    __syncthreads();  
    //this loop is actually fully unrolled  
    for (j = 32 * k; j <= 32 * k + 32; j++) {  
      acpy = acpy + c[j][32 * bx + tx] * bcpy[j];  
    }  
    __syncthreads();  
  }  
  a[tx + 32 * bx] = acpy;  
}
```

BLAS Library Kernel Optimization (SP)

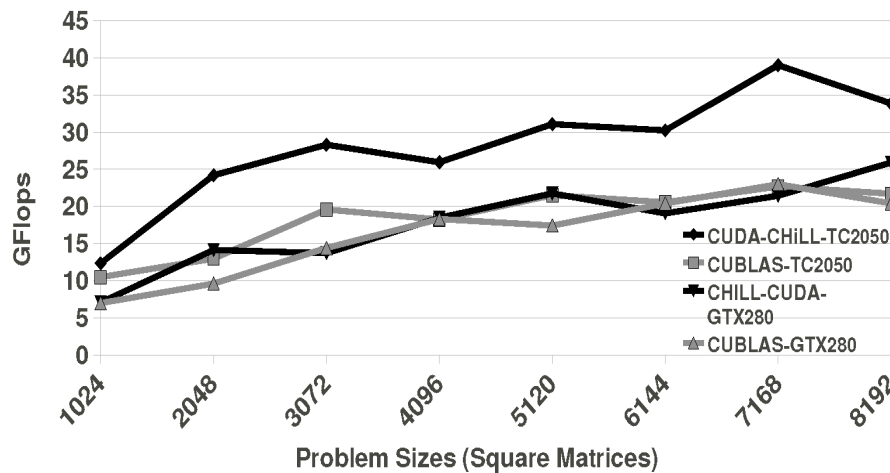
Impact: Sometimes outperforms manually tuned



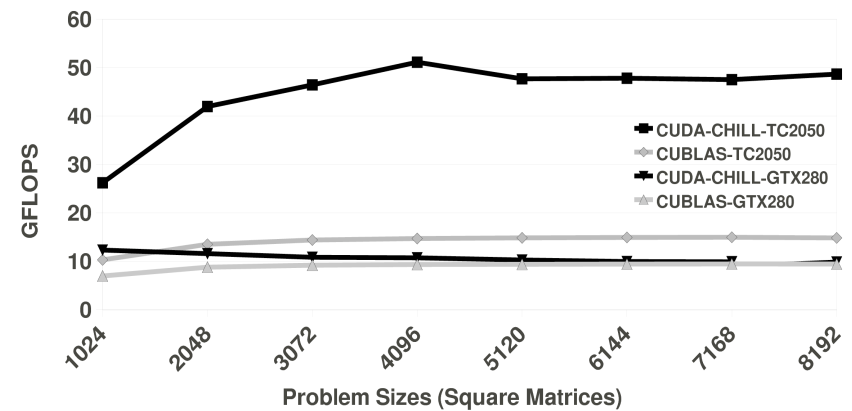
MV Results



MM Results



TMV Results



VV Results

Concluding Remarks

Compiler-based collaborative auto-tuning:

- Track manual tuning research and try to replicate (semi-) automatically
- Express mapping of software to hardware at a high level
- Explore a well-defined search space through empirical techniques
- Portable code generation, and start on heterogeneous support

Case study: linear algebra

- Code + set of transformation recipes target different architectures

Relationship to hardware design space exploration

- Systematic evaluation of many possible implementations
- Rapid evaluation and search space pruning essential